

1) Using the information below, find a formula for  $\vec{x}_{B_2}$ . That is, find the vector  $\vec{x}$  expressed in  $B_2$  coordinates. No need to simplify anything.

$$B_1 = \left\{ \begin{bmatrix} -1 \\ 1 \\ -1 \end{bmatrix}, \begin{bmatrix} 2 \\ 5 \\ 0 \end{bmatrix}, \begin{bmatrix} 4 \\ 2 \\ 1 \end{bmatrix} \right\}, B_2 = \left\{ \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}, \begin{bmatrix} 7 \\ 6 \\ 5 \end{bmatrix}, \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix} \right\}, \vec{x} = \begin{bmatrix} 3 \\ 4 \\ 5 \end{bmatrix}_{B_1}$$

2) A linear operator  $T$  takes input from  $\mathbb{R}^7$ . It is known that there is a vector  $\vec{b}$  such that  $T(\vec{x}) = \vec{b}$  has at least 4 solutions. List all possible values for  $\dim(\text{Col}([T]))$ . That is, list all possible values for the dimension of the column space of the matrix associated to  $T$ .